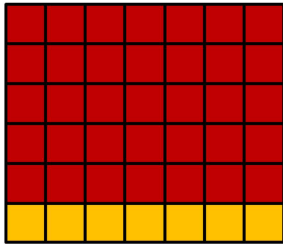


CALCULATION POLICY FOR MULTIPLICATION AND DIVISION **YEAR 6**

Year 6 - Block 1 $6 \times 7 = 42$

7 × table (r)

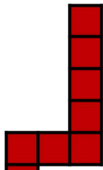


ALL: $6 \times 7 = 42$
PARTS: $5 \times 7 = 35$
 $1 \times 7 = 7$

distributive property of multiplication
reinforced through partitioned array

| × | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
|----|---|---|---|---|---|---|---|---|---|----|
| 1 | | | | | | | | | | |
| 2 | | | | | | | | | | |
| 3 | | | | | | | | | | |
| 4 | | | | | | | | | | |
| 5 | | | | | | | | | | |
| 6 | | | | | | | | | | |
| 7 | | | | | | | | | | |
| 8 | | | | | | | | | | |
| 9 | | | | | | | | | | |
| 10 | | | | | | | | | | |

commutative property



finding missing products on parts
of the multiplication grids

| |
|----|
| 77 |
| 84 |

EFFECTIVE MATHS
139
EFFECTIVE MATHS

BLOCK 1
× AND ÷ UNIT 1

7 × table (r)

Revision of the 7 × table consolidates understanding from earlier year groups. This includes the distributive property of multiplication, through partitioning arrays:

$$6 \times 7 = 5 \times 7 + 1 \times 7.$$

The distributive property allows a factor in a multiplication expression to be decomposed into two or more numbers, and those numbers can be multiplied by the other factor in the multiplication expression.

Children’s understanding of the commutative property is developed through interpreting representations on multiplication grids in two ways, eg:

$$6 \times 7 = 42$$

$$7 \times 6 = 42$$

Understanding about the multiplication grid is deepened through challenging tasks involving finding missing products on parts of multiplication grids.

Year 6 - Block 1

$44 \times 8 = 352$

Efficient strategies for multiplication

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 4 | 4 | × | 8 | = | | | |
| 4 | 0 | × | 8 | = | 3 | 2 | 0 |
| | 4 | × | 8 | = | 3 | 2 | |
| | | | | | 3 | 5 | 2 |

partitioning the first factor

| | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|
| 4 | 4 | × | 8 | = | | | | | |
| 4 | 4 | × | 2 | × | 2 | × | 2 | = | |
| | 8 | 8 | × | 2 | × | 2 | = | | |
| | | | | | | | | | |
| | 1 | 7 | 6 | × | 2 | = | 3 | 5 | 2 |

using factors

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 2 | 2 | × | 1 | 6 | = | | |
| 4 | 4 | × | 8 | = | 3 | 5 | 2 |

using relationships

| | | | | | | | | | | |
|---|---|---|----|---|---|---|---|---|---|---|
| 4 | 4 | × | 8 | = | | | | | | |
| 4 | 4 | × | 10 | - | 8 | 8 | = | | | |
| | 4 | 4 | 0 | - | 8 | 8 | = | 3 | 5 | 2 |

using compensation



Efficient strategies for multiplication

Some calculations, often those with larger numbers, may be best solved with column methods. Understanding about how multiplication works is enhanced through familiarity with a range of methods, which also support mental calculation with smaller numbers.

Efficient strategies for multiplication include:

- column methods;
- partitioning methods;
- factors;
- relationships;
- compensation.

Certain calculations will lend themselves more readily to one or more of the above, so encouraging proficiency in more than one method is important. It also deepens understanding.

Year 6 - Block 1

$216 \div 6 = 36$

Efficient strategies for division

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 2 | 1 | 6 | ÷ | 6 | = | | |
| 1 | 8 | 0 | ÷ | 6 | = | 3 | 0 |
| | 3 | 6 | ÷ | 6 | = | | 6 |
| | | | | | | 3 | 6 |

partitioning the dividend

| | | | | | | | |
|---|---|---|---|---|---|---|-------|
| 2 | 1 | 6 | ÷ | 6 | = | | |
| 2 | 1 | 6 | ÷ | 2 | ÷ | 3 | = |
| | | | | | | | |
| | | 1 | 0 | 8 | ÷ | 3 | = 3 6 |

using factors

| | | | | | | | |
|-----|---|---|---|---|---|---|-----|
| ÷ 2 | 2 | 1 | 6 | ÷ | 6 | = | |
| | 1 | 0 | 8 | ÷ | 3 | = | 3 6 |

using relationships -
multiplicative change to the
dividend and the divisor (scaled
down by 2) meaning the resulting
quotient is also scaled

| | | | | | | | |
|-----|---|---|---|---|---|-----|--|
| ÷ 3 | 2 | 1 | 6 | ÷ | 6 | = | |
| | 7 | 2 | ÷ | 2 | = | 3 6 | |

using relationships -
multiplicative change to the
dividend and the divisor (scaled
down by 3) meaning the resulting
quotient is also scaled

Efficient strategies for division

As with multiplication, some calculations, often those with larger numbers, may be best solved with column methods. Understanding about how division works is enhanced through familiarity with a range of methods, which also support mental calculation with smaller numbers.

Efficient strategies for division include:

- column methods;
- partitioning methods;
- factors;
- relationships.

Year 6 - Block 1

Additional understanding about division

| | | | | | | | | | |
|-----|---|---|---|---|---|---|---|---|--|
| | 2 | 1 | 6 | ÷ | 6 | = | 3 | 6 | |
| ÷ 2 | 1 | 0 | 8 | ÷ | 6 | = | 1 | 8 | |
| ÷ 2 | 5 | 4 | ÷ | 6 | = | | 9 | | |
| ÷ 2 | 2 | 7 | ÷ | 6 | = | | 4 | 5 | |

multiplicative change to the dividend and the divisor remains the same, the quotient changes by the same scale factor

| | | | | | | | | | |
|--|---|---|---|---|-----|---|---|---|---|
| | 2 | 1 | 6 | ÷ | 6 | = | 3 | 6 | |
| | 2 | 1 | 6 | ÷ | 3 | = | 7 | 2 | |
| | 2 | 1 | 6 | ÷ | 1.5 | = | 1 | 4 | 4 |
| | | | | | | | | | |

multiplicative decrease to the divisor and the dividend remains the same, the quotient increases by the same scale factor

multiplicative increase to the divisor and the dividend remains the same, the quotient decreases by the same scale factor

Additional understanding about division

Children have learnt about multiplicative change to the dividend **and** the divisor meaning the resulting quotient changes by the same scale factor.

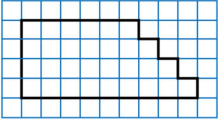
They also learn that:

- if there is a multiplicative change to the dividend and the divisor remains the same, the quotient changes by the same scale factor;
- but if there is a multiplicative decrease to the divisor and the dividend remains the same, the quotient increases by the same scale factor;
- and if there is a multiplicative increase to the divisor and the dividend remains the same, the quotient decreases by the same scale factor.

CALCULATION POLICY FOR MULTIPLICATION AND DIVISION **YEAR 6**

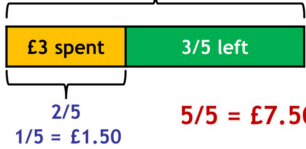
Year 6 - Block 1

Finding fractions of quantities



| | |
|---|--|
| $\frac{1}{3} \text{ of } \pounds 15.00 = \pounds 5.00$ $\frac{1}{6} \text{ of } \pounds 15.00 = \pounds 2.50$ $\frac{5}{6} \text{ of } \pounds 15.00 = \pounds 12.50$ <p style="text-align: center; font-size: small;">procedural variation used to support calculation process</p> |  <p style="text-align: center; font-size: small;">The shape needs to be coloured in as shown below. $\frac{2}{5}$ = red; $\frac{3}{10}$ = orange; $\frac{1}{6}$ = green; $\frac{2}{15}$ = blue. Calculate the number of squares needed for each colour.</p> <p style="text-align: center; font-size: small;">solving increasingly complex problems</p> |
|---|--|

Ling had some money.
 She spent $\pounds 1.10$ on a drink.
 She spent $\pounds 1.90$ on a sandwich.
She has three fifths of her money left.
 How much money did Ling have to start with?

Ling's money



continuing to use bar model representations to support problem solving


144


BLOCK 1
FRACTIONS UNIT 1

Finding fractions of quantities

Children have had lots of experience of finding unit fractions of quantities and, from Year 4, finding non-unit fractions of quantities. The procedure for finding fractions of quantities should be secure.

In Year 6 the emphasis is largely on solving problems involving non-unit fractions of quantities. Intelligent calculation practices are also promoted. For example, finding five-sixths of $\pounds 15$ is not best done by dividing $\pounds 15$ by 6 and multiplying the result by 5. Finding one-sixth is far easier by finding one-third and then halving this to obtain one-sixth. Now five-sixths can be obtained.

CALCULATION POLICY FOR MULTIPLICATION AND DIVISION YEAR 6

Year 6 - Block 1 $792 \div 33 = 24$

Dividing by a 2-digit number using factors and using partitioning

```

graph TD
    A[792] --> B1[330]
    A --> B2[330]
    A --> B3[132]
    B1 -- "÷ 33" --> C1[10]
    B2 -- "÷ 33" --> C2[10]
    B3 -- "÷ 33" --> C3[4]
    C1 --> D[24]
    C2 --> D
    C3 --> D
    
```

$792 \div 33 = 792 \div 3 \div 11$

$$\begin{array}{r} 264 \\ 3 \overline{) 792} \\ \underline{6} \\ 19 \\ \underline{6} \\ 12 \\ \underline{12} \\ 0 \end{array}$$

$264 \div 11 =$

$$\begin{array}{r} 024 \\ 11 \overline{) 264} \\ \underline{22} \\ 44 \\ \underline{44} \\ 0 \end{array}$$

using factors to divide

partitioning the dividend to divide - numeric representation

145

BLOCK 1
× AND ÷ UNIT 2

Dividing by a 2-digit number using factors and using partitioning

Partitioning supports conceptual understanding about division. The dividend is partitioned into parts that are divisible by the divisor. There is no set number of parts to partition the dividend into. In the example shown, using chunks of 330 makes things fairly straightforward.

Dividing by using factors can be effective for situations where the dividend is not a prime number. In the example shown factors of 33 are used. It does not matter which factor becomes the divisor first of all. Here, it makes sense to divide by 3 first and then 11. (NB Dividing 264 by 11 is done using the algorithm for short division.)

CALCULATION POLICY FOR MULTIPLICATION AND DIVISION **YEAR 6**

Year 6 - Block 2

× and ÷ numbers by 10, 100 and 1,000 (r)

3 ÷ 10 →

| Th | H | T | O | t | h | th |
|----|---|---|---|---|---|----|
| | | | 3 | | | |
| | | | 0 | . | 3 | |

3 ÷ 100 →

| Th | H | T | O | t | h | th |
|----|---|---|---|---|---|----|
| | | | 3 | | | |
| | | | 0 | . | 0 | 3 |

3 ÷ 1,000 →

| Th | H | T | O | t | h | th |
|----|---|---|---|---|---|-----|
| | | | 3 | | | |
| | | | 0 | . | 0 | 0 3 |

| | |
|--------------------|---------|
| 5.3×10 | 530 |
| 5.3×100 | 530,000 |
| $5.3 \times 1,000$ | 5,300 |
| 0.53×10 | 53 |
| 530×100 | 53,000 |
| $530 \times 1,000$ | 530,000 |

$230 \div 10 = \square \div 100$
 $230 \div 100 = 23 \div \square$
 $\square \div 1,000 = 2.3 \div 100$

EFFECTIVE
MATHS

147

EFFECTIVE
MATHS

BLOCK 2
MONEY AND DECIMALS UNIT 1

× and ÷ numbers by 10, 100 and 1,000 (r)

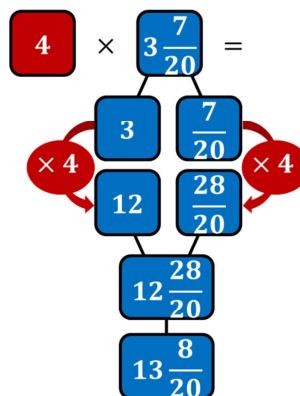
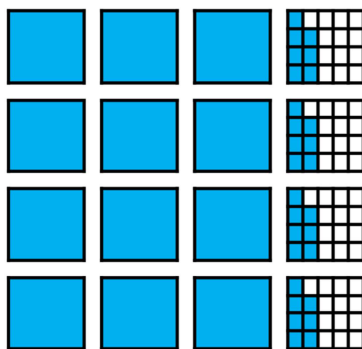
Children revisit multiplying and dividing numbers with up to three decimal places by 10, 100 and 1,000. (This was first encountered in Year 5, × and ÷ unit 2.) The place value chart is used to highlight what happens to the digits when we multiply or divide by 10, 100 and 1,000. Activities require children to think carefully about multiplicative relationships when multiplying and dividing by 10, 100 and 1,000.

Year 6 - Block 2

Multiplying proper fractions and mixed numbers by whole numbers (r)

$$\frac{8}{10} + \frac{8}{10} + \frac{8}{10} = \frac{8}{10} \times 3 = \frac{24}{10} = 2\frac{4}{10}$$

multiplying proper fractions by whole numbers



multiplying mixed fractions by whole numbers



**BLOCK 2
FRACTIONS UNIT 2**

Multiplying proper fractions and mixed numbers by whole numbers (r)

Teaching about the multiplication of fractions begins by revisiting learning from Year 5 about multiplying fractions by whole numbers.

Multiplying proper fractions by whole numbers

The focus here is on understanding that we multiply the numerator by the whole number; we do not multiply the denominators. Repeated addition is used to help reinforce the concept: eight-tenths plus eight-tenths plus eight-tenths = twenty-four tenths = 2 and four-tenths

Multiplying mixed fractions by whole numbers

Partition 3 7/20 into whole parts and fractional parts.

Multiply the wholes.

Multiply the fractional parts.

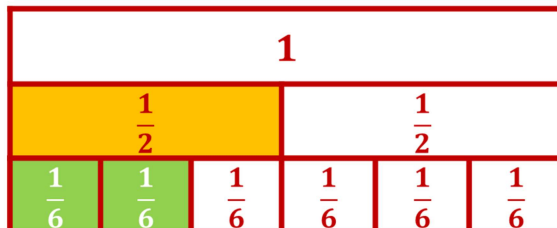
Combine.

The initial combining results in the non-conventional format of a mixed number with an improper fractional part. In this instance, 12 28/20. Whilst this is structurally correct, explain that convention means we write the mixed number so the numerator is less than the denominator.

Year 6 - Block 2

Multiplying pairs of proper fractions

$$\frac{2}{3} \times \frac{1}{2} = \frac{2}{6} = \frac{1}{3}$$



$$\frac{2}{3} \text{ of } \frac{1}{2} = \frac{2}{6} = \frac{1}{3}$$

conceptual understanding is developed by explaining how multiplication equations connect to visual representations

EFFECTIVE
MATHS

149

EFFECTIVE
MATHSMultiplying pairs of proper fractions

Learning about multiplying pairs of proper fractions begins with addressing the misconception that multiplication makes things bigger. Teaching highlights that multiplication can make things bigger, result in no change or can make things smaller.

$$2 \times 2 = 4$$

$$1 \times 1 = 1$$

$$\frac{1}{2} \times \frac{1}{2} = \frac{1}{4}$$

Teaching highlights the varied vocabulary used for the multiplication symbol and teaches children that one word that can be used for it is 'of'.

$$\frac{1}{2} \text{ of } \frac{1}{2} = \frac{1}{4}$$

Children learn the rules for multiplying pairs of proper fractions.

[1] Multiply the numerators of the fractions to get the new numerator.

[2] Multiply the denominators of the fractions to get the new denominator.

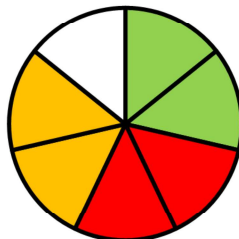
[3] Simplify if needed.

Conceptual understanding is developed by explaining how multiplication equations connect to visual representations.

Year 6 - Block 2

Dividing a fraction by a whole number

(dividend is a fraction - divisor is a whole number - numerator is a multiple of the whole number)



numerator
is a
multiple of the
whole number

$$\frac{6}{7} \div 3 = \frac{2}{7}$$

dividend is a
fraction divisor
is a whole
number

Dividing a fraction by a whole number

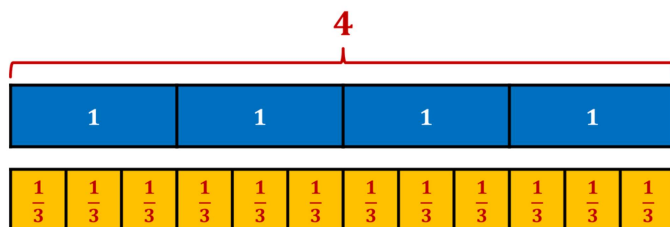
Learning to divide a fraction by a whole number begins with examples where the dividend is a fraction, the divisor is whole number and the numerator is a multiple of the whole number. For example:

$$6/7 \div 3.$$

Pictorial representations support conceptual understanding that we are not dividing the denominator. Children need to understand that the denominator tells us about the size of the parts and the numerator tells us how many parts there are.

Year 6 - Block 2

Dividing a whole number by a unit fraction
 (dividend is a whole number - divisor is a fraction)



$$4 \div \frac{1}{3} = 12$$

dividend divisor
 is a is a
 whole fraction
 number

EFFECTIVE
MATHS

151

EFFECTIVE
MATHS

Dividing a whole number by a unit fraction

Now the examples have the dividend as a whole number and the divisor is a fraction. For example:

$$4 \div 1/3.$$

Pictorial representations support conceptual understanding. The key teaching point here is about visualising how many thirds are ‘inside’ the dividend.

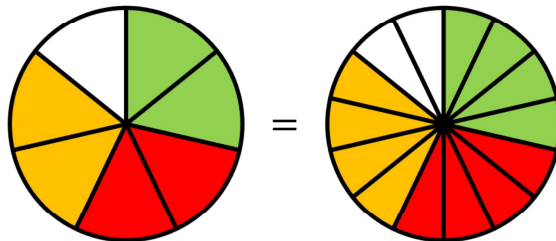
Start by getting the children to think about how many thirds are in one. Then build that up to how many thirds are in two, three and four.

Highlight the relationship between the **whole number** and the **denominator**.

Finally, ask if it can be solved another way.

- Decimal equivalents. These will not be useful here as we are dividing by one-third. However they would be if the calculation were $4 \div \frac{1}{4}$, for example.
- Scaling. Multiply the fraction by 3 to obtain 1, resulting in: $12 \div 1 = 12$.

Year 6 - Block 2

Dividing a fraction by a whole number(dividend is a fraction - divisor is a whole number - numerator is *not* a multiple of the whole number)

numerator
is *not* a
multiple of the whole number -
so we need an equivalent fraction where the numerator is: twelve-fourteenths

$$\frac{6}{7} \div 4 = \frac{3}{14}$$

dividend
is a
fraction

divisor
is a
whole
number

Dividing a fraction by a whole number

The final step in learning to divide a fraction by a whole number involves examples where the dividend is a fraction, the divisor is whole number and the numerator is *not* a multiple of the whole number. For example:

$$6/7 \div 4.$$

Teaching helps children to understand that we need to find an equivalent fraction (in this case 12/14) where we can divide the numerator by the denominator. Pictorial representations support conceptual understanding of this process.

CALCULATION POLICY FOR MULTIPLICATION AND DIVISION **YEAR 6**

Year 6 - Block 3

Derive related calculations

if one factor is multiplied by a number, then the other factor must be divided by the same number for the product to stay the same

$0.4 \times 240 = 4 \times \square$

$0.6 \times 180 = 6 \times \square$

$800 \times 120 = 96,000$

$80 \times 120 = 9,600$

$8 \times 120 = 960$

$0.8 \times 120 = 96$

$0.08 \times 120 = 9.6$

if one factor is multiplied by a number, and the other factor kept the same, then the product must be multiplied by the same number

EFFECTIVE MATHS 153 EFFECTIVE MATHS

BLOCK 3
CALCULATION UNIT

Derive related calculations

Children have used the compensation property of multiplication previously, for example, when recognising connections between multiplication table facts:

$5 \times 8 = 10 \times 4.$

They have also used it as method to simplify calculations:

$22 \times 16 = 44 \times 8.$

This learning is consolidated and children secure learning that if one factor is multiplied by a number, then the other factor must be divided by the same number for the product to stay the same. They use this knowledge to complete equations such as $0.4 \times 240 = 4 \times \square$ and, more generally, to help them simplify calculations.

Children have learnt to scale known number facts by 10, 100, one-tenth and one-hundredth. They know that if one factor is multiplied by a number, and the other factor kept the same, then the product must be multiplied by the same number. This knowledge is applied to solve missing number problems and also as a method to simplify calculations.